

ORIGIN := 1

$$T := 332.4 \quad x := \begin{pmatrix} 0.73 \\ 0.27 \end{pmatrix}$$

i represents components, Acetone = 1, Benzene = 2

$i := 1 .. 2$

j represents functional groups, CH3 = 1, CH3CO = 2, ACH = 3

$j := 1 .. 3$

R and Q values for the functional groups

$$R := \begin{pmatrix} 0.9011 \\ 1.6724 \\ 0.5313 \end{pmatrix} \quad Q := \begin{pmatrix} 0.848 \\ 1.488 \\ 0.400 \end{pmatrix}$$

vij is the number of functional group j present in component i

$$v := \begin{pmatrix} 1 & 1 & 0 \\ 0 & 0 & 6 \end{pmatrix}$$

$$r_i := \sum_j (v_{i,j} \cdot R_j) \quad q_i := \sum_j (v_{i,j} \cdot Q_j)$$

$$\Phi_i := \frac{r_i \cdot x_i}{\sum_i (r_i \cdot x_i)} \quad \theta_i := \frac{q_i \cdot x_i}{\sum_i (q_i \cdot x_i)} \quad l_i := 1 - r_i + 5(r_i - q_i)$$

Combinatorial Activity Coefficient

$$\ln \gamma_{C_i} := \ln \left(\frac{\Phi_i}{x_i} \right) + 5 q_i \cdot \ln \left(\frac{\theta_i}{\Phi_i} \right) + l_i - \frac{\Phi_i}{x_i} \cdot \left[\sum_i (x_i \cdot l_i) \right]$$

Interaction Parameters

$$a := \begin{pmatrix} 0 & 476.4 & 61.13 \\ 26.76 & 0 & 140.1 \\ -11.12 & 25.77 & 0 \end{pmatrix}$$

$$m := 1 \dots 3 \quad n := 1 \dots 3$$

$$\Psi_{m,n} := \exp\left(\frac{-a_{m,n}}{T}\right)$$

Calculation of total Γ

$$x_j := \frac{\left[\sum_i (v_{i,j} \cdot x_i) \right]}{\left[\sum_j \left[\sum_i (v_{i,j} \cdot x_i) \right] \right]}$$

$$\Theta_j := \frac{Q_j \cdot x_j}{\sum_j (Q_j \cdot x_j)}$$

$$\ln \Gamma_i := Q_j \cdot \left[1 - \ln \left[\sum_m (\Theta_m \cdot \Psi_{m,j}) \right] - \sum_m \frac{\Theta_m \cdot \Psi_{j,m}}{\sum_n (\Theta_n \cdot \Psi_{n,m})} \right]$$

Calculation of Γ for individual groups

$$x_{1j} := \frac{v_{1,j}}{\left(\sum_j v_{1,j} \right)}$$

$$\Theta_{1j} := \frac{Q_j \cdot x_{1j}}{\sum_j (Q_j \cdot x_{1j})}$$

$$k := 1 \dots 2$$

$$\ln \Gamma_{1k} := Q_k \cdot \left[1 - \ln \left[\sum_m (\Theta_{1m} \cdot \Psi_{m,k}) \right] - \sum_m \frac{\Theta_{1m} \cdot \Psi_{k,m}}{\sum_n (\Theta_{1n} \cdot \Psi_{n,m})} \right]$$

$$\ln \Gamma_2 := 0$$

Residual Activity Coefficient

$$\ln \gamma_{R1} := \sum_k [v_{1,k} \cdot (\ln \Gamma_k - \ln \Gamma_{1k})]$$

$$\ln \gamma_{R2} := \sum_m [v_{2,m} \cdot (\ln \Gamma_m - \ln \Gamma_2)]$$

Activity Coefficient of Species

$$\gamma_i := \exp(\ln \gamma_{C_i} + \ln \gamma_{R_i})$$

$$\gamma = \begin{pmatrix} 1.0395 \\ 1.2538 \end{pmatrix}$$