

ORIGIN := 1

a := 1      This represents methane to steam mole ratio

$$n_{\text{CH}_4}(\varepsilon_1, \varepsilon_2) := 1 - \varepsilon_1 - \varepsilon_2$$

$$n_{\text{H}_2\text{O}}(\varepsilon_1, \varepsilon_2) := a - \varepsilon_1 - 2\varepsilon_2$$

$$n_{\text{CO}}(\varepsilon_1, \varepsilon_2) := \varepsilon_1$$

$$n_{\text{CO}_2}(\varepsilon_1, \varepsilon_2) := \varepsilon_2$$

$$n_{\text{H}_2}(\varepsilon_1, \varepsilon_2) := 3\varepsilon_1 + 4\varepsilon_2$$

$$n(\varepsilon_1, \varepsilon_2) := n_{\text{CH}_4}(\varepsilon_1, \varepsilon_2) + n_{\text{H}_2\text{O}}(\varepsilon_1, \varepsilon_2) + n_{\text{CO}}(\varepsilon_1, \varepsilon_2) + n_{\text{CO}_2}(\varepsilon_1, \varepsilon_2) + n_{\text{H}_2}(\varepsilon_1, \varepsilon_2)$$

$$\varepsilon_1 := 0.1 \quad \varepsilon_2 := 0.1$$

Given

$$0.031 = 4 \cdot \left( \frac{n_{\text{CO}}(\varepsilon_1, \varepsilon_2) \cdot n_{\text{H}_2}(\varepsilon_1, \varepsilon_2)^3}{n_{\text{CH}_4}(\varepsilon_1, \varepsilon_2) \cdot n_{\text{H}_2\text{O}}(\varepsilon_1, \varepsilon_2) \cdot n(\varepsilon_1, \varepsilon_2)^2} \right)$$

$$0.096 = 4 \cdot \left( \frac{n_{\text{CO}_2}(\varepsilon_1, \varepsilon_2) \cdot n_{\text{H}_2}(\varepsilon_1, \varepsilon_2)^4}{n_{\text{CH}_4}(\varepsilon_1, \varepsilon_2) \cdot n_{\text{H}_2\text{O}}(\varepsilon_1, \varepsilon_2)^2 \cdot n(\varepsilon_1, \varepsilon_2)^2} \right)$$

$$\begin{pmatrix} \varepsilon_1 \\ \varepsilon_2 \end{pmatrix} := \text{Find}(\varepsilon_1, \varepsilon_2) = \begin{pmatrix} 0.055 \\ 0.147 \end{pmatrix}$$

$$y_{\text{CH}_4} := \frac{n_{\text{CH}_4}(\varepsilon_1, \varepsilon_2)}{n(\varepsilon_1, \varepsilon_2)} = 0.332$$

$$y_{\text{H}_2\text{O}} := \frac{n_{\text{H}_2\text{O}}(\varepsilon_1, \varepsilon_2)}{n(\varepsilon_1, \varepsilon_2)} = 0.271$$

$$y_{\text{CO}} := \frac{n_{\text{CO}}(\varepsilon_1, \varepsilon_2)}{n(\varepsilon_1, \varepsilon_2)} = 0.023$$

$$y_{\text{CO}_2} := \frac{n_{\text{CO}_2}(\varepsilon_1, \varepsilon_2)}{n(\varepsilon_1, \varepsilon_2)} = 0.061$$

$$y_{\text{H}_2} := \frac{n_{\text{H}_2}(\varepsilon_1, \varepsilon_2)}{n(\varepsilon_1, \varepsilon_2)} = 0.313$$

$$\alpha := \begin{pmatrix} -1 & -1 & 1 & 3 & 0 & 0 \\ -1 & -2 & 0 & 4 & 1 & 0 \\ 0 & 0 & -2 & 0 & 1 & 1 \\ 0 & 1 & -1 & -1 & 0 & 1 \\ -1 & 0 & 0 & 2 & 0 & 1 \end{pmatrix}$$

$$\text{rank}(\alpha) = 3$$

$$y_{\text{CO}} := 0.01 \quad y_{\text{H}_2} := 0.3 \quad y_{\text{CH}_4} := 0.1 \quad y_{\text{H}_2\text{O}} := 0.3 \quad y_{\text{CO}_2} := 0.1 \quad n := 5$$

Given

$$0.031 = \frac{y_{\text{CO}} \cdot y_{\text{H}_2}^3 \cdot 2^2}{y_{\text{CH}_4} \cdot y_{\text{H}_2\text{O}}}$$

$$0.096 = \frac{y_{\text{CO}_2} \cdot y_{\text{H}_2}^4 \cdot 2^2}{y_{\text{CH}_4} \cdot y_{\text{H}_2\text{O}}^2}$$

$$108 = \frac{y_{\text{CO}_2}}{y_{\text{CO}}^2} \cdot \frac{1}{2^2}$$

$$y_{\text{CH}_4} + y_{\text{H}_2\text{O}} + y_{\text{CO}} + y_{\text{H}_2} + y_{\text{CO}_2} = 1$$

$$4y_{\text{CH}_4} + 2y_{\text{H}_2\text{O}} + 2y_{\text{H}_2} = \frac{6}{n}$$

$$y_{\text{H}_2\text{O}} + y_{\text{CO}} + 2y_{\text{CO}_2} = \frac{1}{n}$$

$$\text{Find}(y_{\text{CH}_4}, y_{\text{H}_2\text{O}}, y_{\text{CO}}, y_{\text{H}_2}, y_{\text{CO}_2}, n) = \begin{pmatrix} 0.257 \\ 0.324 \\ 0.012 \\ 0.373 \\ 0.034 \\ 2.477 \end{pmatrix}$$